

# Estimating the mass of solar type stars

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# Estimating the mass of solar type stars

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Additional thanks:

**O. Creevey (Institut d'Astrophysique Spatiale), A. Mortier<sup>4</sup>**

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/SFRH/BPD/37491/2007**

# Mass inference methods<sup>1</sup>

## 1) Surface gravity:

$$\log(g) = 4.4377506 + \log\left(\frac{M}{M_{\odot}}\right) / \left(\frac{R}{R_{\odot}}\right)^2$$
$$\frac{R}{R_{\odot}} = F(L, T_{\text{eff}})$$

## 2) Torres et al. (2010, A&A Rev., 18, 67)

$$\log(M/M_{\odot}) = 1.5689 + 1.3787X + 0.4243X^2 + 1.139X^3$$
$$-0.1425(\log g)^2 + 0.01969(\log g)^3 + 0.1010[\text{Fe}/X]$$
$$X = \log(T_{\text{eff}}) - 4.1$$

## 3) Henry & McCarthy (1993, AJ, 106, 77)

$$\log(M/M_{\odot}) = 0.002456 M_v - 0.09711 M_v + 0.4365$$

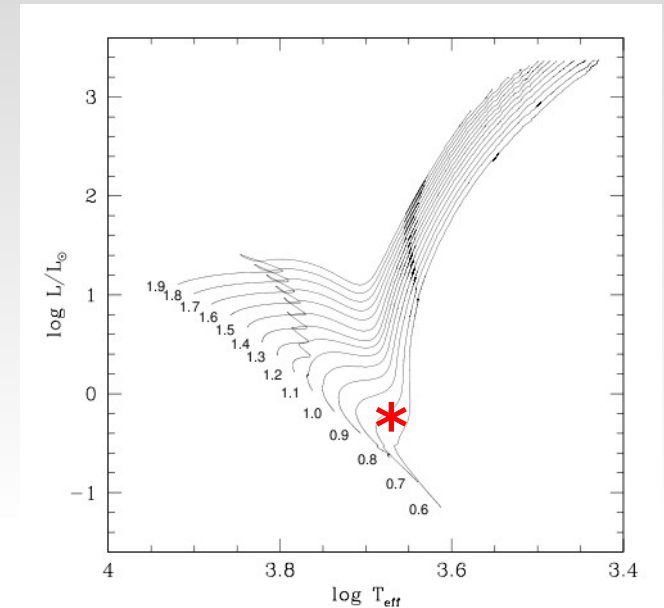
$$M_v = F(L, T_{\text{eff}}) \text{ from Torres (2010, AJ, 140, 1158)}$$

# Mass inference methods<sup>2</sup>

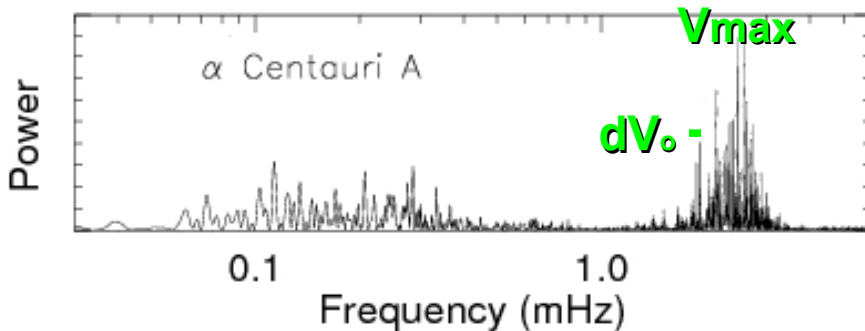
## 4) Padova Models

(Girardi et al., 2000, A&AS, 141, 371)

$$\min_{\substack{X = T_{\text{eff}}, L/L_{\odot}, \log(g), [Fe/X]}} \sum \frac{X_{\text{star}} - X_{\text{model}}}{\text{err} X_{\text{star}}}$$



## Asteroseismology:

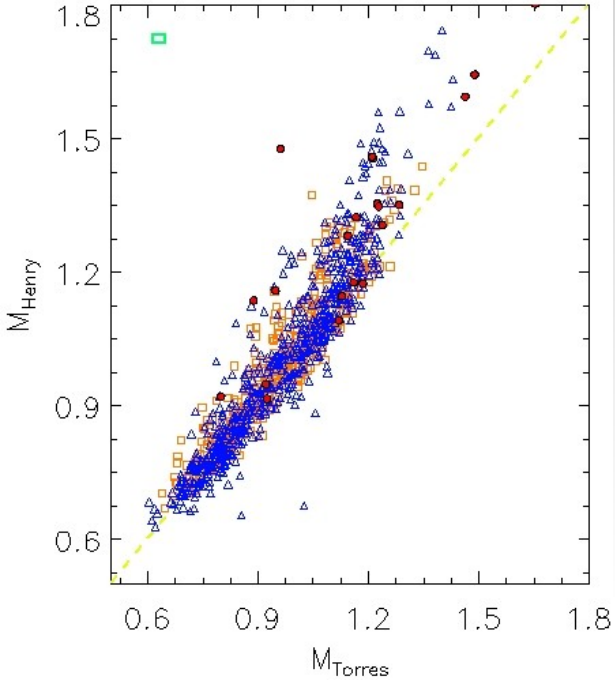


$$dV_0 = \sqrt{(M/M_{\odot}) / (R/R_{\odot})^3} \times 0.1349 \text{ mHz}$$

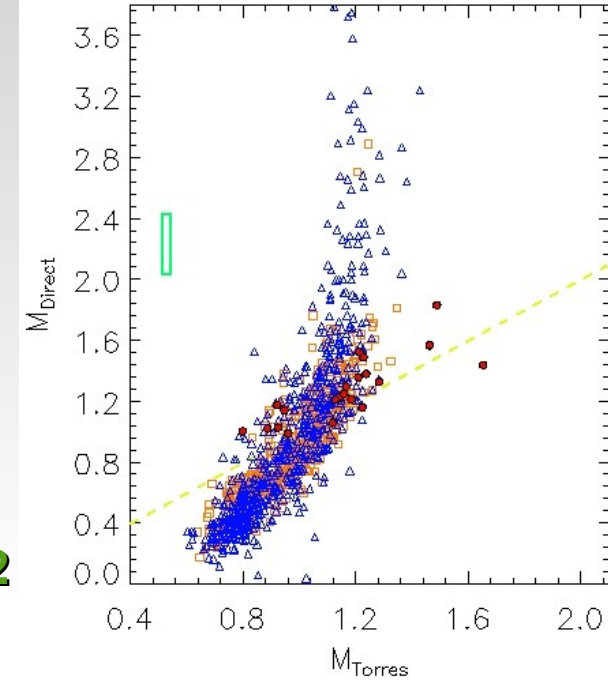
$$V_{\text{max}} = \frac{M/M_{\odot}}{(R/R_{\odot})^2 \sqrt{T_{\text{eff}} / 5777}} \times 3.05 \text{ mHz}$$

(Kjeldsen & Bedding, 1995, A&A, 293, 87)

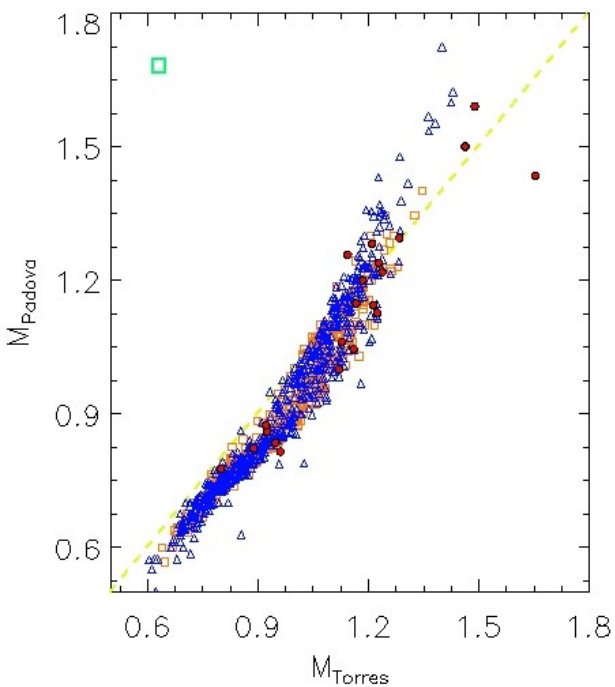
# Comparison between estimates



$$M_H = 1.17 M_T - 0.13 \quad M_{Sp} = 3.24 M_T - 2.12$$

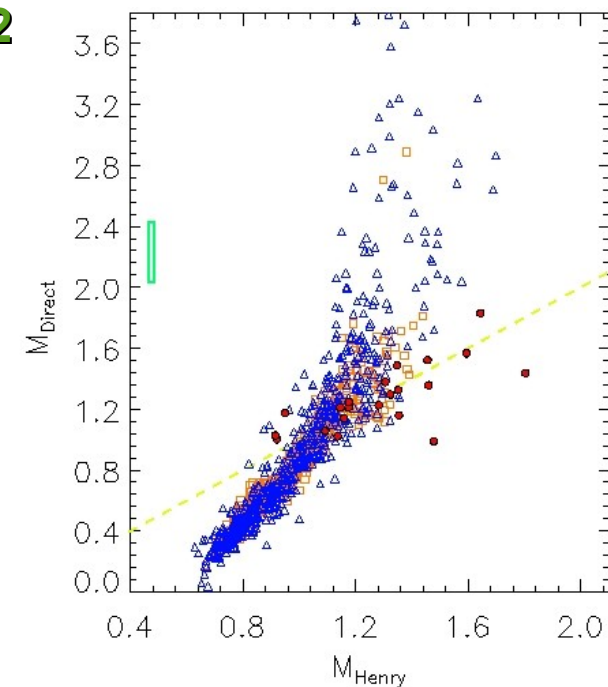


$$M_P = 1.17 M_T - 0.21 \quad M_{Sp} = 2.81 M_H - 1.82$$



- Sousa et al. 2008  
541\*s; spectroscopic log(g)
- Sousa et al. 2011  
582\*s; spectroscopic log(g)
- Bruntt et al. 2010  
22 \*s; asteroseismic log(g)

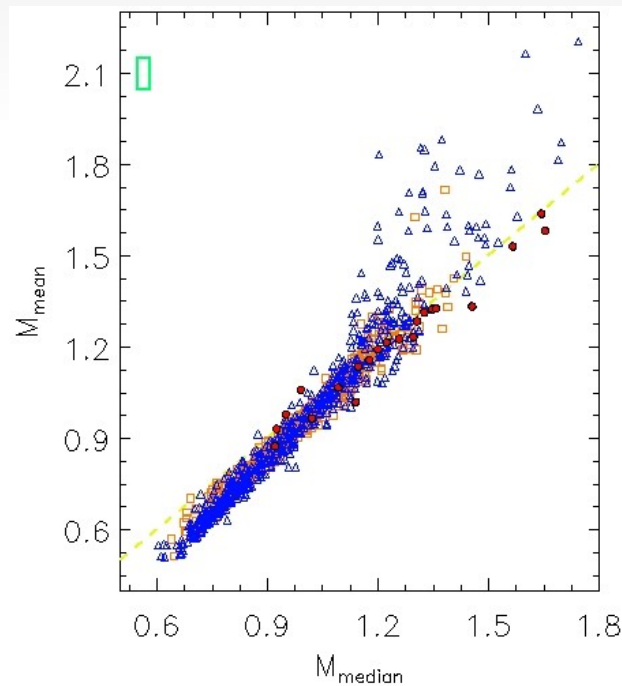
(known: L, Teff, log(g), [Fe/X],  $\pi$ )



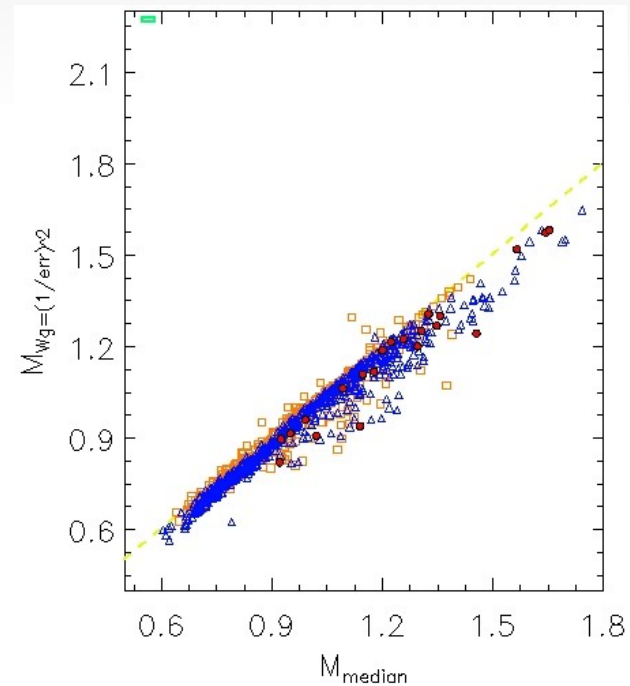
# Combining mass estimates

$$\frac{\sum_{i=1,4} M_i w_i}{\sum_{i=1,4} w_i} \left\{ \begin{array}{l} W_i: \\ 1 \\ 1/(\text{err})^2 \\ Q_i/(\text{err})^2 \\ \dots \end{array} \right. \begin{array}{l} \text{mean} \\ \text{weighted mean} \\ \text{, } Q_i = \text{quality factor} \end{array}$$

$M_u < M_v < M_w < M_x$   
↓  
**Median**

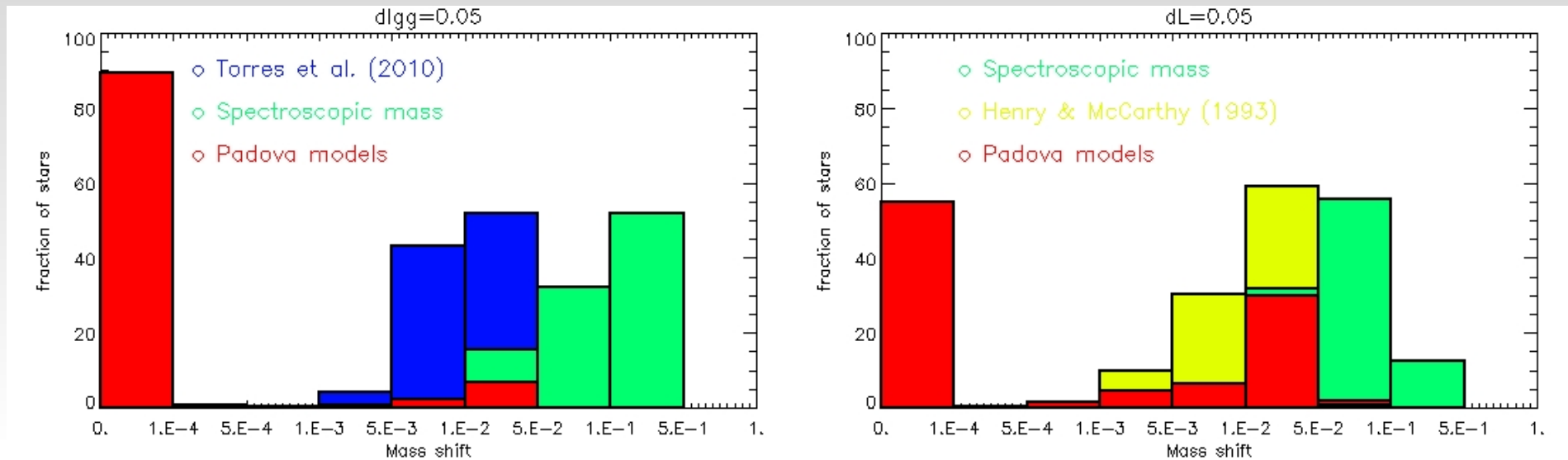


**Mean: more sensitive to outliers (duh!)**



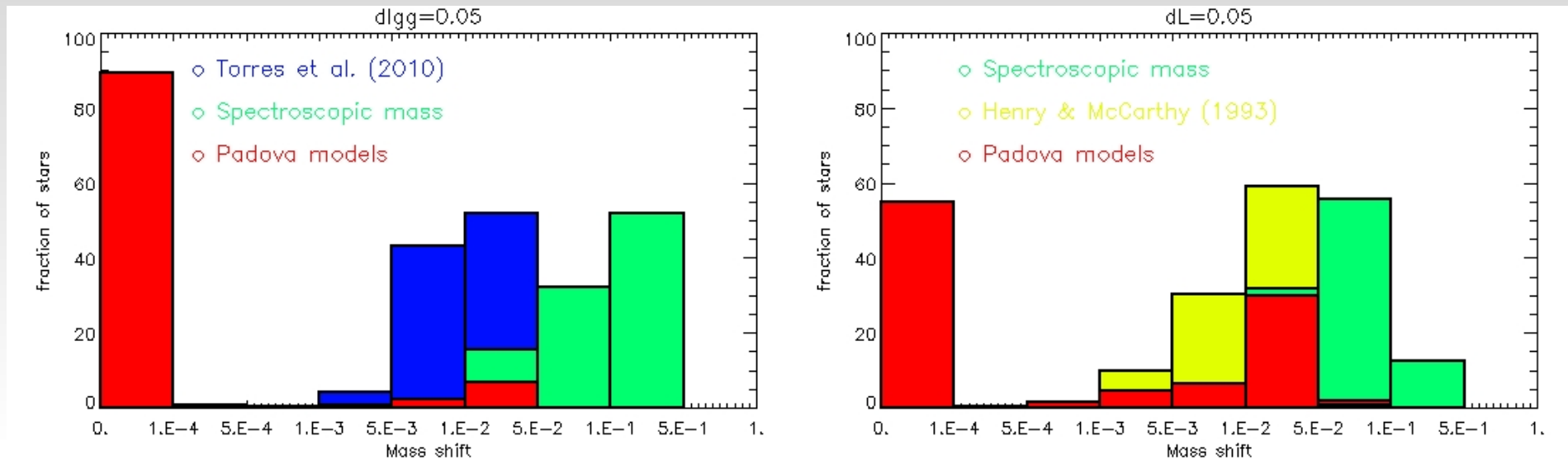
**Good agreement between median and weighted mean**

# Understanding the differences<sup>1</sup>

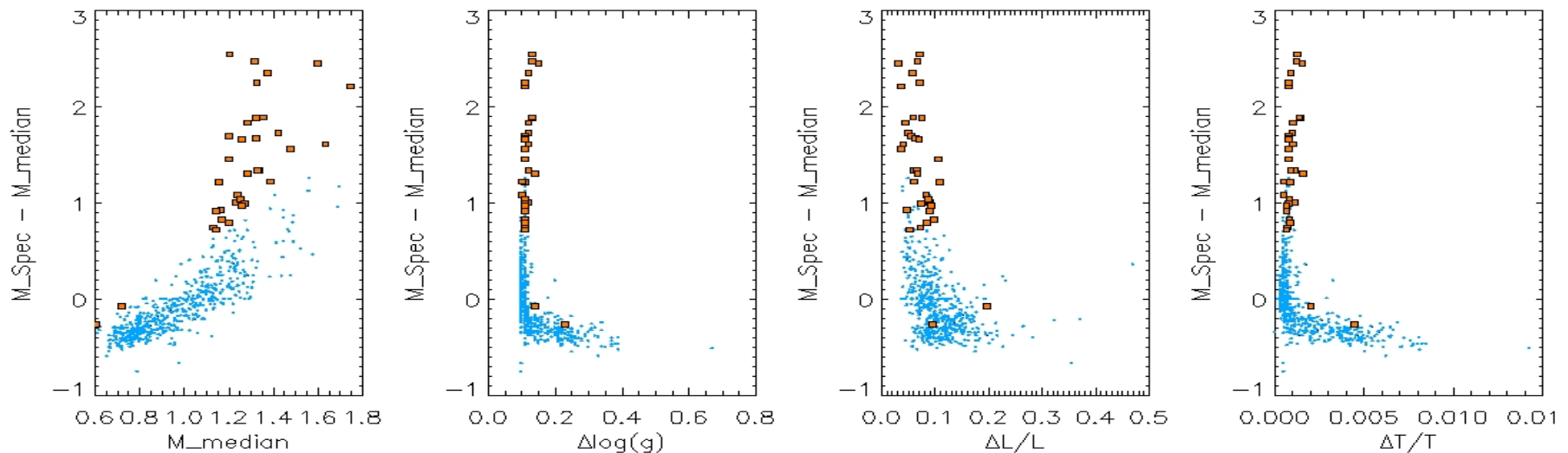


**“Direct” method seems more sensitive to errors in L & log(g)**

# Understanding the differences<sup>1</sup>



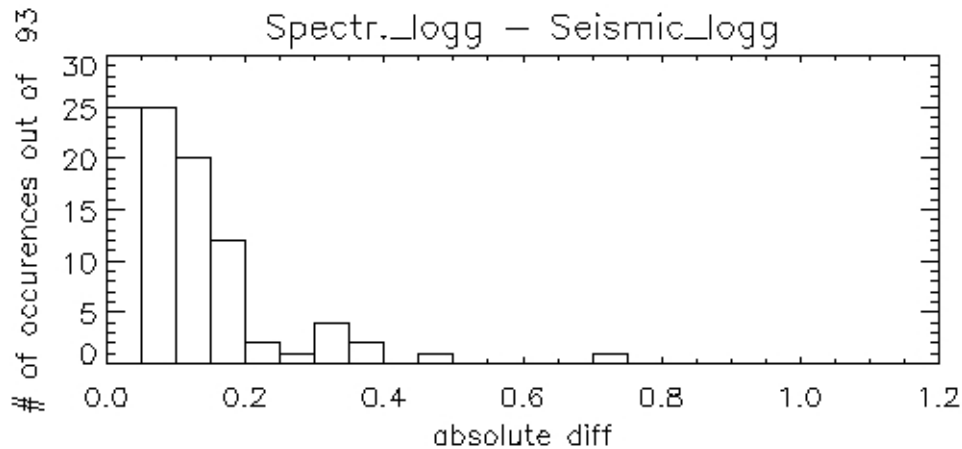
**“Direct” method seems more sensitive to errors in L & log(g)**



**Found no errors in input parameters that justify such differences**



# Understanding the differences<sup>2</sup>

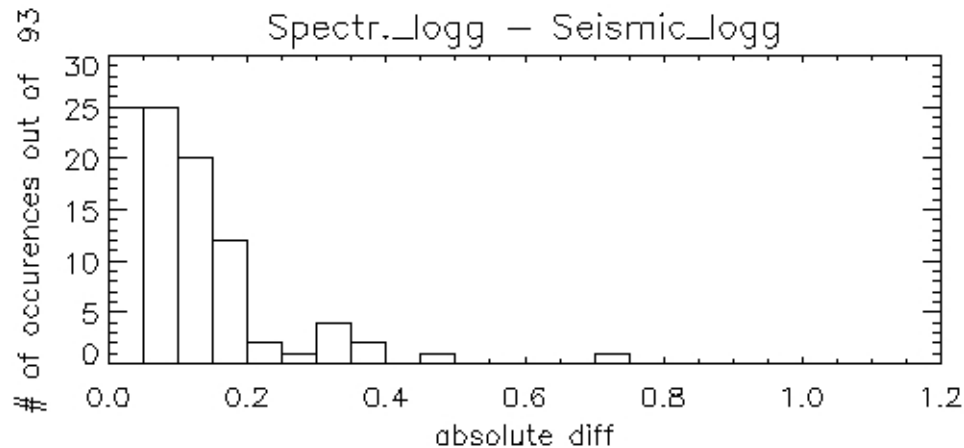


Bruntt et al., 2012, MNRAS, 423, 122  
(KEPLER's data)



**Is there a problem with spectroscopic  $\log(g)$ ?**

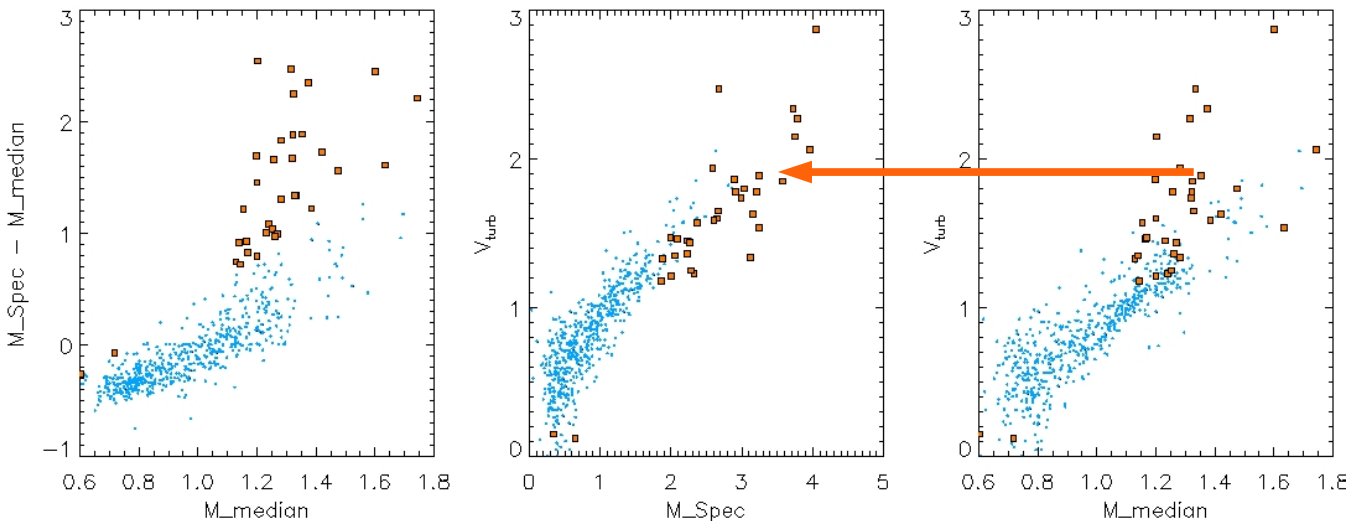
# Understanding the differences<sup>2</sup>



Bruntt et al., 2012, MNRAS, 423, 122  
(KEPLER's data)



**Is there a problem with spectroscopic log(g)?**



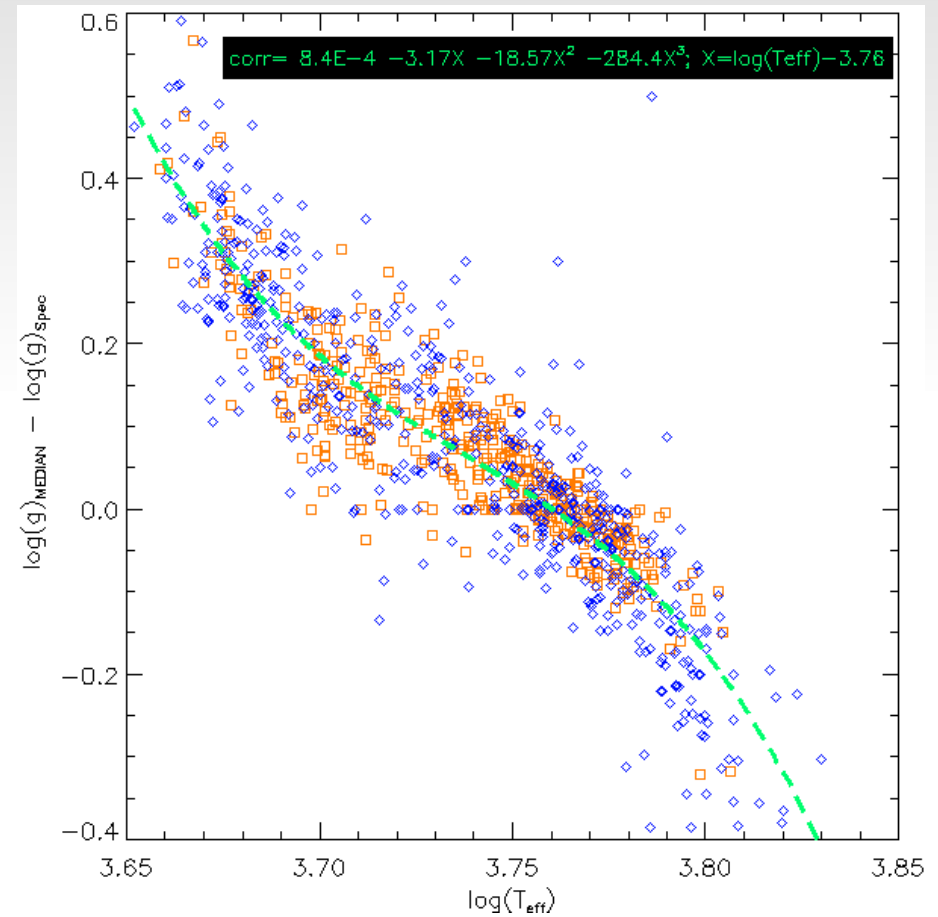
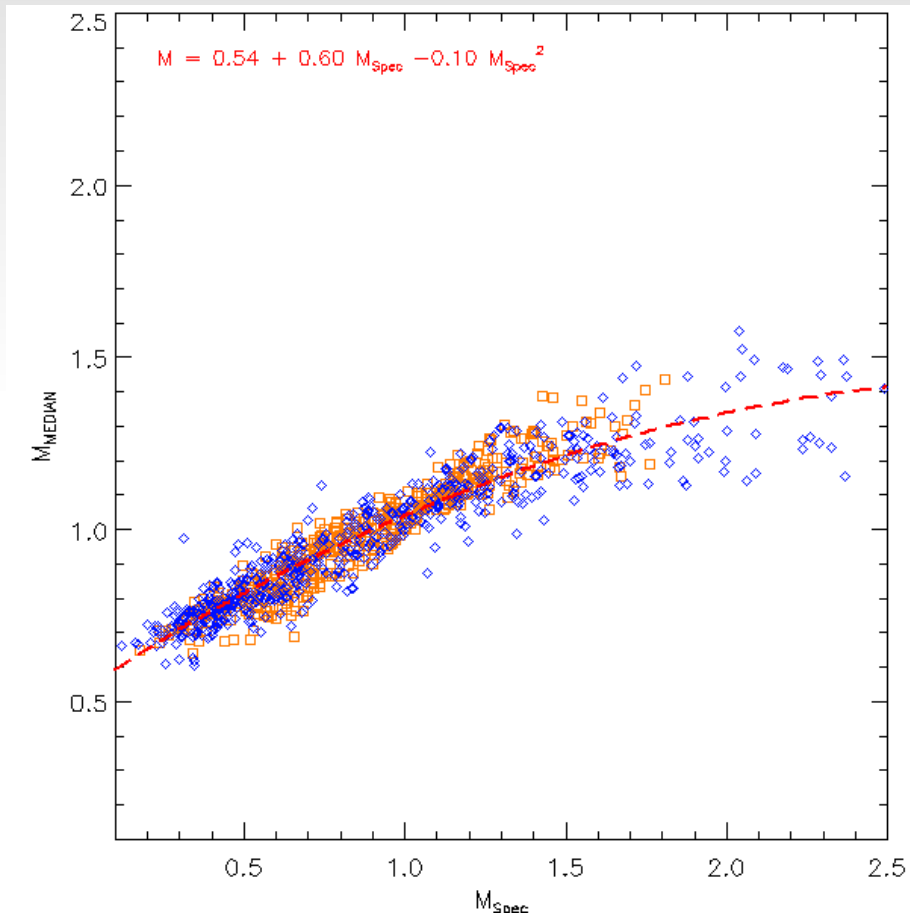
**Problem with  $V_{\text{turb}}$ ?**

**Beware:**

**$V_{\text{turb}} - T_{\text{eff}}$  correl.**

**$M - L - T_{\text{eff}}$  correl. @MS**

# Empirically "adjusting" the spectroscopic predictions



# Conclusions

- **Good agreement between Torres, Henry & Padua's predictions**
- **A bit less for the spectroscopic masses.**
- **Median & weighted mean good ways of combining masses**
  
- **Observed systematic difference (non-random) between the spectroscopic predictions and those of the remaining methods**
  
- **Physical reason for this difference?**  
(perhaps  $V_{\text{turb}}$  or 3D vs 1D atmospheric models?)
  
- **That difference can be empirically corrected**

***Thank you!***